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# Forecasting: Methods and Applications

Makridakis, Spyros

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# FORECASTING

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Methods and Applications  
Third Edition

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